

Free Particle Propagation.

Given an initial wavefunction $\Psi(x,0)$, find the future evolution of the free-particle wavefunction $\Psi(x,t)$

Griffiths Problem 2.20

Here we calculate the time evolution of the wavefunction from part (c) of the question

$$\Psi(x,t) = \frac{a^{3/2}}{\pi} \int \frac{1}{a^2 + k^2} e^{i(kx - \hbar k^2 t / 2m)} dk$$

We take $a = 1$ and $\hbar/2m = 1$ for simplicity in the calculations that follow.

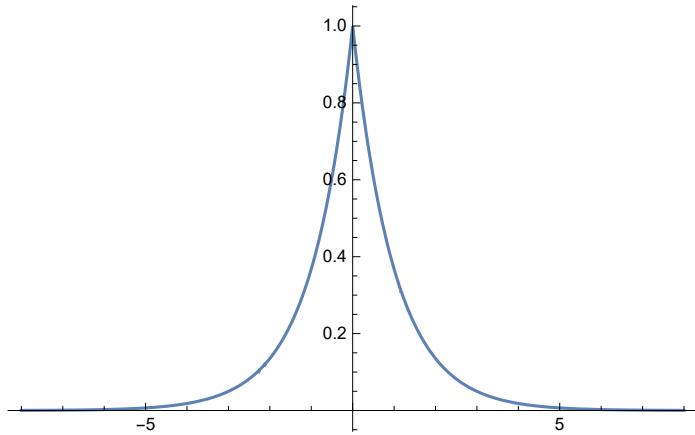
```
In[1]:= Ψ[x_, t_] := 1/π NIntegrate[1/(1 + k^2) Exp[I (k x - k^2 t)], {k, -∞, ∞}]
```

```
In[2]:= Ψ[0, 0]
```

```
Out[2]= 1.
```

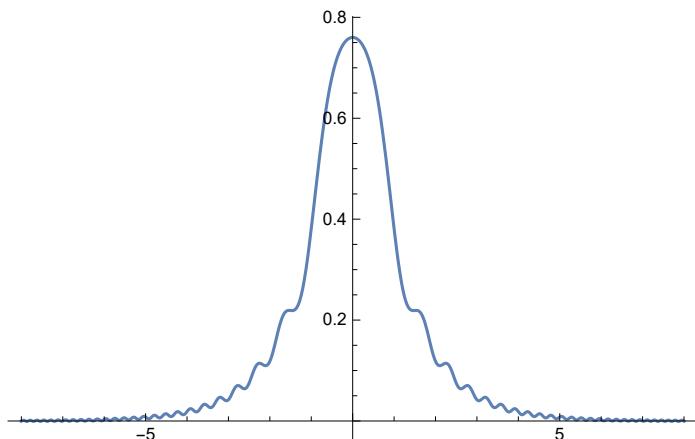
```
In[3]:= plot0 = Plot[Re[Ψ[x, 0]], {x, -8, 8}, PlotRange → All]
(* Wavefunction at t = 0, i.e. the initial wavefunction *)
```

```
Out[3]=
```



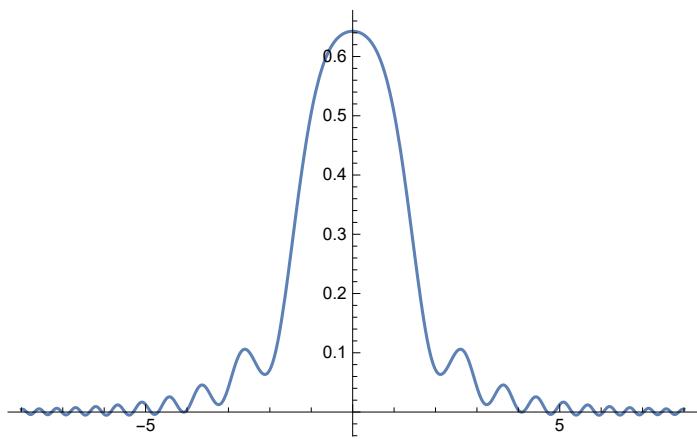
```
In[4]:= plotp1 = Plot[Re[Ψ[x, 0.1]], {x, -8, 8}, PlotRange → All] (* Wavefunction at t = 0.1 *)
```

```
Out[4]=
```



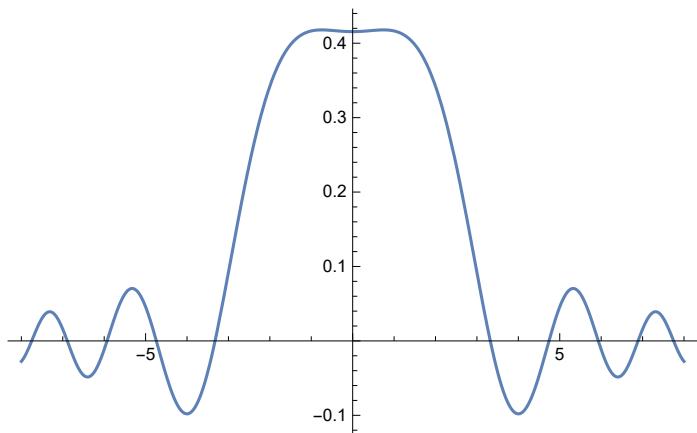
```
In[5]:= plotp25 = Plot[Re[\Psi[x, 0.25]], {x, -8, 8}, PlotRange -> All]
(* Wavefunction at t = 0.25 *)
```

Out[5]=



```
In[6]:= plot1 = Plot[Re[\Psi[x, 1]], {x, -8, 8}, PlotRange -> All] (* Wavefunction at t = 1 *)
```

Out[6]=



```
In[7]:= Show[plot0, plotp1, plotp25, plot1] (* Overlay of wavefunctions at t = 0, 0.1, 0.25, 1 *)
```

Out[7]=

